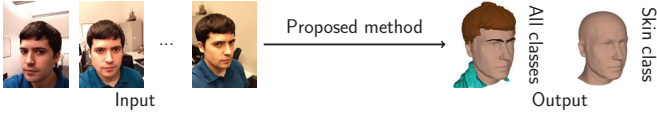


# Semantic 3D Reconstruction of Heads

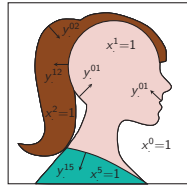
## Introduction

We propose a system that automatically reconstructs and semantically segments human heads from images taken in uncontrolled environments using a multi-label shape prior



## Formulation

- Labeling of a voxel space into  $L$  labels  $x_s^i \in [0, 1]$  and  $\sum_i x_s^i = 1$
- Labels: free space, skin, hair, eyebrows, beard and clothing
- Unary cost contains depth information
- Smoothness cost depends on surface orientation and involved labels (contains shape prior and semantic information)



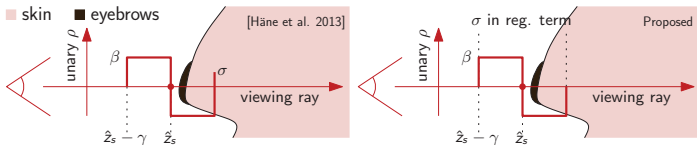
## Optimization Problem

$$E(\mathbf{x}, \mathcal{T}) = \sum_{s \in \Omega} \left( \sum_i \rho_s^i(\mathcal{T}) x_s^i + \frac{1}{\alpha^2} \sum_{i,j:i < j} \phi_s^{ij}(\mathcal{T}, x_s^i - x_s^j) \right)$$

$$\text{s. t. } x_s^i = \sum_j (x_s^j)_{e_k}, \quad x_s^j = \sum_j (x_s^j)_{e_k}, \quad \sum_i x_s^i = 1, \quad x_s^i \geq 0, \quad x_s^j \geq 0.$$

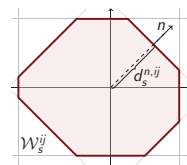
- $x_s^i \in [0, 1]$ : indicates whether label  $i$  is chosen at voxel  $s$
- $y_s^{ij} = x_s^i - x_s^j \in [-1, 1]^3$ : presence of a surface and its direction
- $\rho_s^i$ : unary term, cost for label  $i$  at location  $s$
- $\phi_s^{ij}$ : convex smoothness term at voxel  $s$  for labels  $i$  and  $j$
- $e_k \in \mathbb{R}^3$ :  $k$ -th canonical basis vector
- $\mathcal{T}$ : alignment between prior and input data
- $\alpha$ : normalization factor for scale
- Convex in  $\mathbf{x}$ , not convex in  $\mathcal{T}$  (optimized using alternating optimization)

## Unary Term



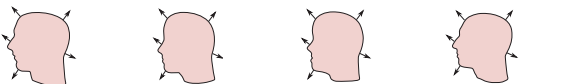
## Data Dependent Regularization Term

- Smoothness term  $\phi_s^{ij}(\cdot)$  in terms of a convex Wulff shape  $\mathcal{W}_s^{ij}$ , approximated as intersection of half spaces
- $d_s^{n,ij}$ : cost for surface with normal direction  $n$  between labels  $i$  and  $j$ , corresponds to distance of half space boundary to origin
- We have  $\phi_s^{ij} = d_s^{n,ij}$
- $d_s^{n,ij} = -\log(P(n_s^{ij} | \mathcal{T}, \Gamma))$  is approximated with



$$\tilde{d}_s^{n,ij} := \underbrace{w_s^{ij}(\mathcal{T}, \Gamma)}_{\text{semantic weight}} \underbrace{\left( -\log(P(n_s^{ij} | \leftarrow \rightarrow)) \right)}_{\text{normal based shape prior}} \underbrace{\left( -\log(P(\leftarrow \rightarrow | \rightarrow)) \right)}_{\text{transition prior}} \underbrace{\left( -\log(P(\leftarrow \rightarrow)) \right)}_{\text{surface prior}}$$

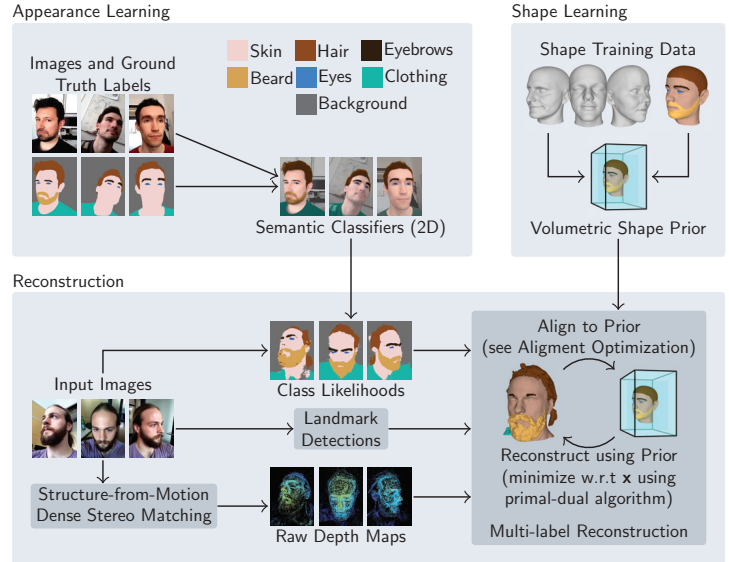
- Normal based shape prior: locally, surface normals are similar between different heads



- General Wulff shape replaced by surrogate when all normals point in similar direction



## Overview



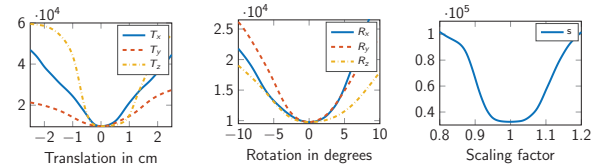
## Alignment Optimization

- Align visible geometry, transitions from free space to skin (more generally multiple classes)
- Formulated as energy over surface

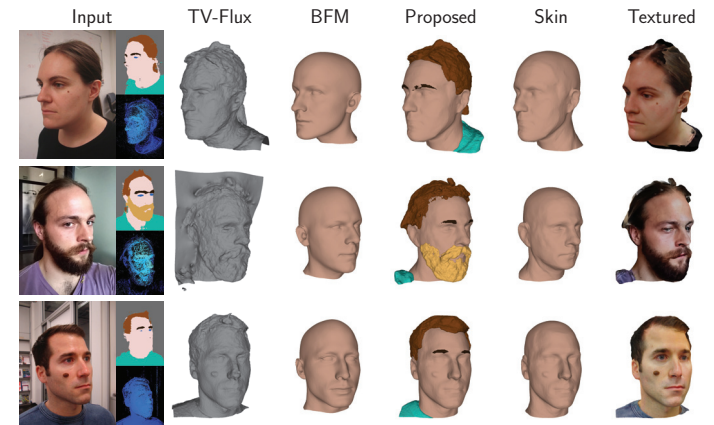
$$E_{\text{mesh}}(\mathcal{T}) = \sum_{t \in \mathbb{T}} \phi_t(\mathcal{T}, n_t(\mathcal{T})) \frac{A_t(\mathcal{T})}{\alpha^2} = \sum_{t \in \mathbb{T}} \phi_t(\mathcal{T}, n_t(\mathcal{T})) A_t(\mathcal{I})$$

- $\mathbb{T}$ : set of triangles
- $\phi_t(\mathcal{T}, n_t(\mathcal{T}))$ : smoothness over triangle  $t$  with normal  $n_t(\mathcal{T})$
- $A_t(\mathcal{I})$ : area of triangle  $t$
- Gradient descent minimization with respect to  $\mathcal{T}$

- Energy plots for translation, rotation and scaling for fixed geometry:



## Results



## Acknowledgment

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