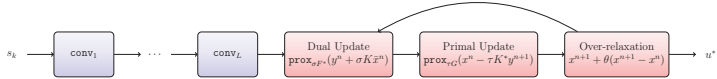


Motivation and Contribution

- Time-of-Flight sensors produce depth maps that are usually of low-resolution and contain severe noise.



- For color images, machine learning based methods for single image super-resolution are highly successful [6, 11, 16].
 - Training data is easy to obtain.
- For depth data, methods are mostly based on energy minimization [5, 7].
 - Piece-wise affine surfaces.
 - Sharp depth discontinuities.



- Unroll variational method with anisotropic Total Generalized Variation [2] regularization on top of a deep network.
- Train method end-to-end on huge set of synthetically generated depth maps.
- Code and data is published on GitHub
<https://github.com/griegler/primal-dual-networks>



ATGV-Net

- Formulated as bi-level optimization problem [14, 15]:

$$\min_w \frac{1}{K} \sum_{k=1}^K L(u^*(f(w, s_k)), t_k) \quad (\text{HL})$$

$$\text{s.t. } u^*(f(w, s_k)) = \arg \min_u E(u; f(w, s_k)). \quad (\text{LL})$$

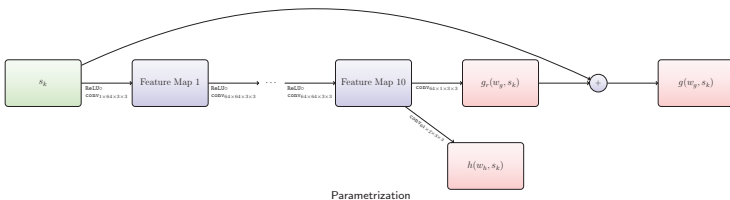
- Energy functional with anisotropic TGV as in [7]
 - Emphasizes piece-wise affine surfaces.
 - Convex optimization problem.

$$E(u; f(w, s_k)) = R(u, h(w_h, s_k)) + \frac{e^{w_\lambda}}{2} \|u - g(w_g, s_k)\|_2^2 \quad (1)$$

$$R(u, h(w_h, s_k)) = \min_v \alpha_1 \|T(h(w_h, s_k))(\nabla u u - v)\|_1 + \alpha_0 \|\nabla v\|_1. \quad (2)$$

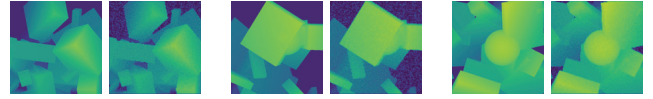
- Unroll primal-dual optimization scheme [3] on top of deep network.
 - Joint training with deep network.
 - Regularization term parameterized by additional network output.
 - Learning of optimization hyper-parameters for each step.

$$\begin{cases} p^{n+1} = \text{proj}(p^n + \sigma_p \alpha_1 (T(h(w_h, s_k))(\nabla u \bar{u}^n - \bar{v}^n))) \\ q^{n+1} = \text{proj}(q^n + \sigma_q \alpha_0 \nabla v \bar{v}^n) \\ u^{n+1} = \frac{u^n + \tau_u (\alpha_1 \nabla_v^T T(h(w_h, s_k)) p^{n+1} + e^{w_\lambda} g(w_g, s_k))}{1 + \tau_u e^{w_\lambda}} \\ v^{n+1} = v^n + \tau_v (\alpha_0 \nabla_v^T q^{n+1} + \alpha_1 T(h(w_h, s_k)) p^{n+1}) \\ \bar{u}^{n+1} = u^{n+1} + \theta(u^{n+1} - u^n) \\ \bar{v}^{n+1} = v^{n+1} + \theta(v^{n+1} - v^n). \end{cases} \quad (3)$$



Training Data

- Generating training data by ray tracing cubes and spheres in 3D.



Evaluation on Noise-Free Data

- Evaluation on Middlebury disparity maps as proposed by [1].

	$\times 2$				$\times 4$			
	Cones	Teddy	Tsukuba	Venus	Cones	Teddy	Tsukuba	Venus
NN	4.3772	3.2596	9.7968	2.1408	6.1236	4.5168	13.3248	2.9432
Bicubic	3.8392	2.7668	8.3648	1.8192	4.9544	3.5744	10.6960	2.3504
Diebel & Thrun [5]	2.9588	2.1060	6.4208	1.3624	4.5624	3.2040	8.7840	1.9408
Fersti et al. [7]	2.8240	2.1408	7.0592	1.2840	3.6372	2.5068	10.0128	1.4624
Zeyde et al. [19]	2.7680	1.9616	6.1936	1.3200	3.8468	2.7512	8.7632	1.7592
Timofte et al. [17]	2.7872	1.9816	6.1280	1.3328	3.0256	3.0256	9.6304	1.9616
Aodha et al. [1]	4.5076	3.2988	9.6192	2.2088	6.0168	4.1036	13.3328	2.6920
Horn��cek et al. [10]	3.9744	3.1640	9.2832	2.0592	5.5944	4.7828	11.6352	3.6008
Fersti et al. [8]	2.4988	1.7588	5.6064	1.1464	3.7336	2.6680	7.8416	1.8096
CNN only	1.0275	0.8801	2.3610	0.2866	3.0015	1.5330	6.4361	0.4219
CNN + ATGV-L2	1.0145	0.8374	2.3197	0.2720	2.9832	1.5175	6.4223	0.4121
ATGV-Net	1.0021	0.8155	2.2846	0.1991	2.9293	1.5029	6.6327	0.3764

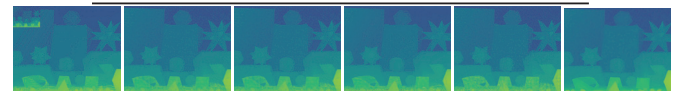


Input & GT Bicubic Horn  cek et al. [10] Fersti et al. [8] CNN only ATGV-Net

Evaluation on Noisy Data

- Middlebury disparity maps with synthetic noise as proposed by [13].

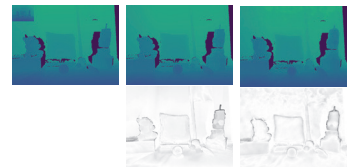
	$\times 2$			$\times 4$		
	Art	Books	Moebius	Art	Books	Moebius
NN	6.55	6.16	6.59	7.48	6.31	6.78
Bilinear	4.58	3.95	4.20	5.62	4.31	4.56
Yang et al. [18]	3.01	1.87	1.92	4.02	2.38	2.42
He et al. [9]	3.55	2.37	2.48	4.41	2.74	2.83
Diebel & Thrun [5]	3.49	2.06	2.13	4.51	3.00	3.11
Chan et al. [4]	3.44	2.09	2.08	4.46	2.77	2.76
Park et al. [13]	3.76	1.95	1.96	4.56	2.61	2.51
Fersti et al. [7]	3.19	1.52	1.47	4.06	2.21	2.03
CNN only	2.02	1.27	1.50	3.55	2.41	2.68
CNN + ATGV-L2	1.93	1.14	1.37	3.40	2.24	2.51
ATGV-Net	1.84	1.13	1.24	2.98	1.72	1.95



Input & GT He et al. [9] Yang et al. [18] Fersti et al. [7] CNN only ATGV-Net

- ToFMarm dataset [7].

	Books	Devil	Shark
NN	30.46	27.53	38.21
Bilinear	29.11	25.34	36.34
Kapf et al. [12]	27.82	24.30	34.79
He et al. [9]	27.11	23.45	33.26
Fersti et al. [7]	24.00	23.19	29.89
ATGV-Net	24.67	21.74	28.51



Input & GT Fersti et al. [7] ATGV-Net

References and Acknowledgment

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